

# *Probing Higgs self-couplings at Future Colliders*

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Mini-Workshop: Theory  
Physics Opportunities and Advanced Tools  
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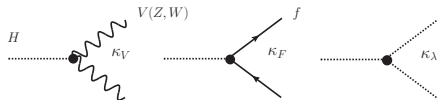
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# Higgs couplings in the SM

The SM Higgs sector is governed by the following Lagrangian,

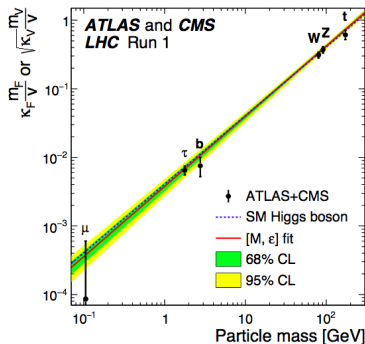
$$\mathcal{L}_{\text{Higgs}} = |D_\mu \Phi|^2 - \sum_f y_f \bar{L}_f \Phi R_f - V(\Phi)$$



- EWSB  $\Rightarrow$  Higgs couplings with gauge bosons ( $\kappa_V$ ), with fermions ( $\kappa_F$ ) and Higgs self-couplings ( $\kappa_\lambda$ )
- *How precisely do we know these couplings?*

$$\kappa_V \sim 10\%, \quad \kappa_F^* \sim 10 - 20\%$$

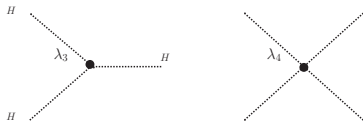
$\kappa_\lambda$  : practically unconstrained!



# SM Higgs potential & New Physics

Higgs potential & EWSB in the SM,

$$\begin{aligned} V^{\text{SM}}(\Phi) &= -\mu^2(\Phi^\dagger\Phi) + \lambda(\Phi^\dagger\Phi)^2 \\ \text{EWSB} \Rightarrow V(H) &= \frac{1}{2}m_H^2 H^2 + \lambda_3 v H^3 + \frac{1}{4}\lambda_4 H^4. \end{aligned}$$



The mass and the self-couplings of the Higgs boson depend only on  $\lambda$  and  $v = (\sqrt{2}G_\mu)^{-1/2}$ ,

$$m_H^2 = 2\lambda v^2; \quad \lambda_3^{\text{SM}} = \lambda_4^{\text{SM}} = \lambda.$$

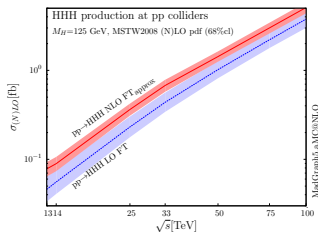
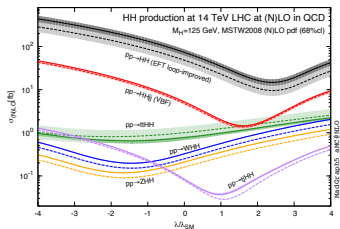
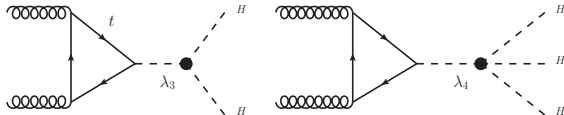
$$m_H = 125 \text{ GeV} \text{ and } v \sim 246 \text{ GeV}, \Rightarrow \boxed{\lambda \approx 0.13}.$$

Presence of new physics at higher energy scales can contribute to the Higgs potential and modify the Higgs self-couplings.

*Independent measurements of  $\lambda_3$  and  $\lambda_4$  are crucial.*

# Direct determination of Higgs self-couplings

Information on  $\lambda_3$  and  $\lambda_4$  can be extracted by studying multi-Higgs production processes.



[Frederix et al. '14, 1408.6542]

Very challenging due to small cross sections:  $\sim 33$  fb ( $HH$ ),  $\sim 0.1$  fb ( $HHH$ )

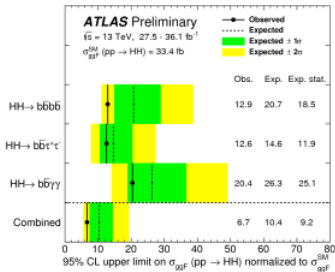
Compare it with the single Higgs production ( $gg \rightarrow H$ ) cross section:  $\sim 50$  pb

# Current experimental sensitivity

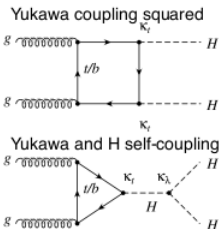
## Di-Higgs production

- ATLAS:  $\mu < 6.7$  (exp 10.4) @95% CL
- CMS:  $\mu < 22$  (exp 13) @95% C.L.
- Limits at 95% CL on self-coupling scale factor  $\kappa_\lambda$ :
  - ATLAS:  $-5.0 < \kappa_\lambda < 12.1$
  - CMS:  $-11.8 < \kappa_\lambda < 18.8$

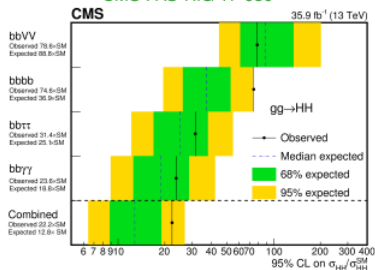
ATLAS-CONF-2018-043



26 November 2018



CMS-PAS-HIG-17-030



Stefano Rosati - Higgs Couplings 2018

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# Future Projections

ATLAS (HL-LHC,  $2b2\gamma$ ): [ATL-PHYS-PUB-2017-001],

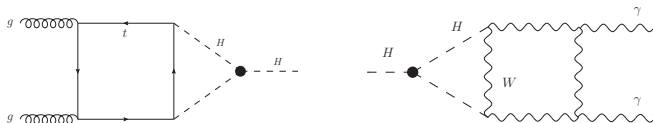
$$\kappa_3 < -0.8 \text{ and } \kappa_3 > \sim 7.7$$

*Bounds are sensitive to  $\kappa_t$  value.*

*Are there alternative methods of probing  $\lambda_3$  and  $\lambda_4$ ?*

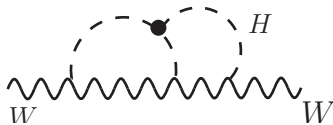
# Indirect determination of $\lambda_3$

- $\lambda$ -dependent corrections to single Higgs processes



- > Gorbahn, Haisch: 1607.03773
- > Degrassi, Giardino, Maltoni, Pagani: 1607.04251
- > Bizon, Gorbahn, Haisch, Zanderighi: 1610.05771
- > Di Vita, Grojean, Panico, Riemann, Vantalon: 1704.01953
- > Maltoni, Pagani, AS, Zhao: 1709.08649

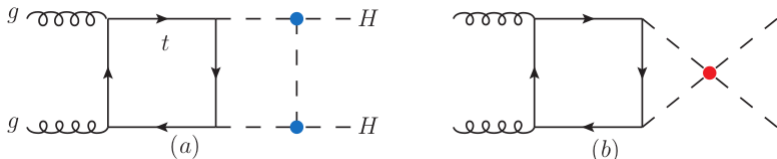
- $\lambda$ -dependent corrections in electroweak precision observables



- > Degrassi, Fedele, Giardino: 1702.01737
- > Kribs, Maier, Rzehak, Spannowsky, Waite: 1702.07678

# Indirect determination of $\lambda_4$

[1810.04665,1811.12366]



NP parametrization

$$V^{\text{NP}}(\Phi) \equiv \sum_{n=3}^{\infty} \frac{c_{2n}}{\Lambda^{2n-4}} \left( \Phi^\dagger \Phi - \frac{1}{2} v^2 \right)^n.$$

$$V(H) = \frac{1}{2} m_H^2 H^2 + \lambda_3 v H^3 + \frac{1}{4} \lambda_4 H^4 + \lambda_5 \frac{H^5}{v} + O(H^6),$$

$$\kappa_3 \equiv \frac{\lambda_3}{\lambda_3^{\text{SM}}} = 1 + \frac{c_6 v^2}{\lambda \Lambda^2} \equiv 1 + \bar{c}_6,$$

$$\kappa_4 \equiv \frac{\lambda_4}{\lambda_4^{\text{SM}}} = 1 + \frac{6c_6 v^2}{\lambda \Lambda^2} + \frac{4c_8 v^4}{\lambda \Lambda^4} \equiv 1 + 6\bar{c}_6 + \bar{c}_8.$$

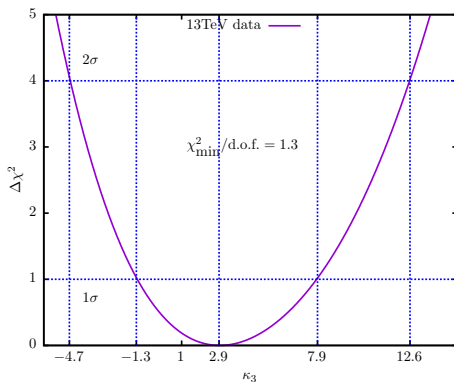


# Single Higgs

# Current reach at the LHC

Studies have confirmed that indirect bounds on  $\lambda_3$  can be competitive with the direct ones. A one parameter fit using **8 TeV LHC data** ([1607.04251](#))  $\Rightarrow$

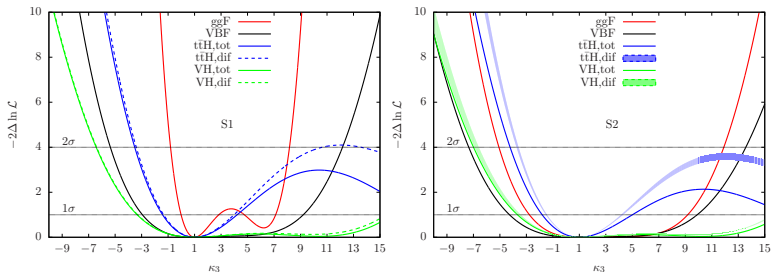
$$-9.4 < \kappa_3 < 17$$



(Plot by Xiaoran)

# Future projections (1P): constraints on $\kappa_3$ ( $\kappa_t = \kappa_V = 1$ )

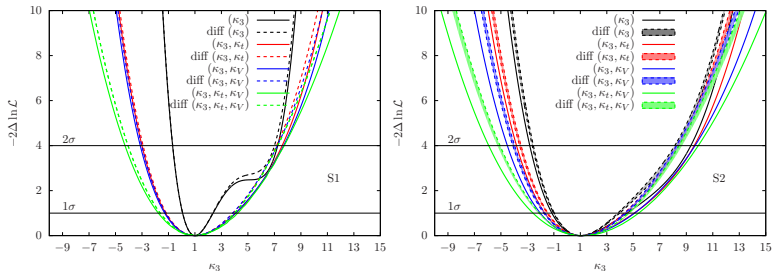
ATLAS-HL: S1 (stat.), S2 (stat. + sys. + th.) *Different production channels*



- In S1 the fit is dominated by the  $ggF$ -like channel. In S2 the  $t\bar{t}H$ -like channel provides best constraints for  $\kappa_3 < 1$ .
- Improvements in bounds due to the use of differential information in  $t\bar{t}H$  are more visible in S2.
- Differential information in  $ggF$  (*not yet available*) would be useful.

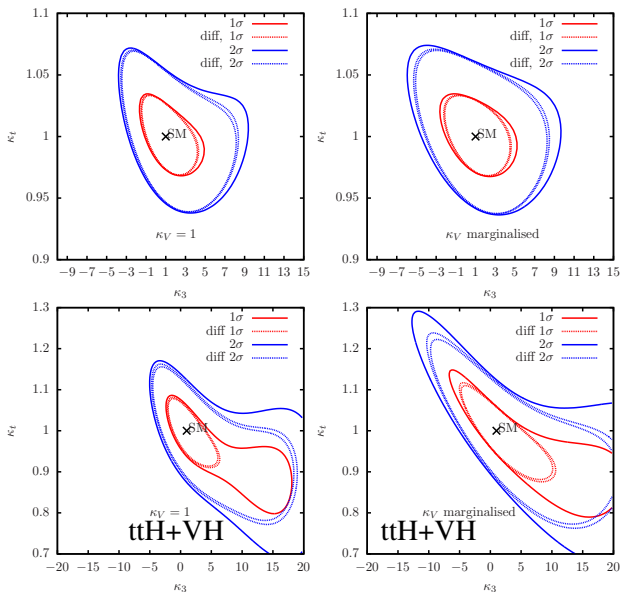
# Future projections(1P): constraints on $\kappa_3$ in presence of $\kappa_t, \kappa_V$

ATLAS-HL: S1 (stat.), S2 (stat. + sys. + th.) *All production channels*

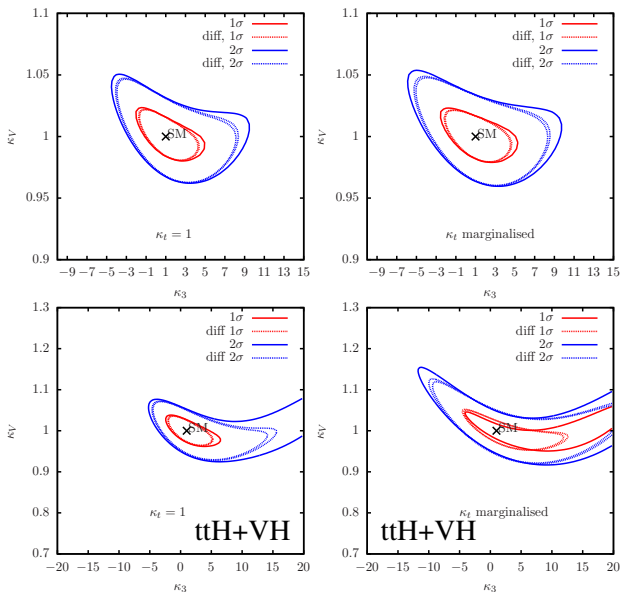


- Inclusion of more parameters to the fit relaxes the constraints especially in the region  $\kappa_3 < 1$ .
- Due to  $\kappa_t$  dependence of the gluon fusion channel, the constraints in presence of  $\kappa_t$  are stronger than those in presence of  $\kappa_V$ .
- Differential information from VH and ttH do improve the bounds in S2.

# Future projections (2P): constraints on $\kappa_3$ and $\kappa_t$ in S2

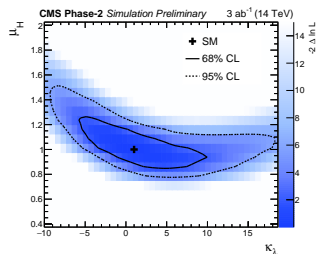
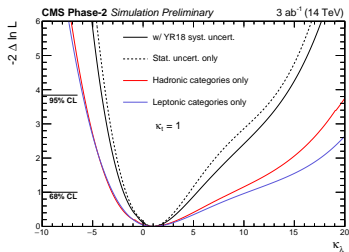


# Future projections (2P): constraints on $\kappa_3$ and $\kappa_V$ in S2



# CMS Projections: HL-LHC

$tH + ttH$



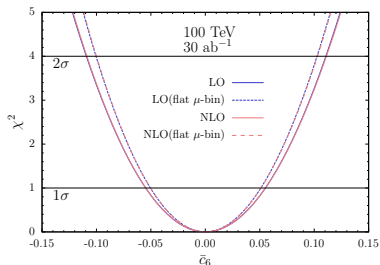
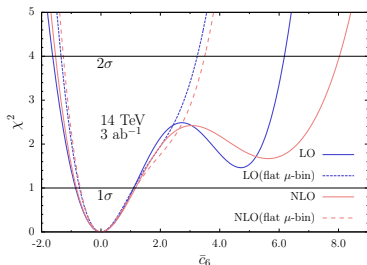
[CMS-PAS-FTR-18-020]

# Double Higgs



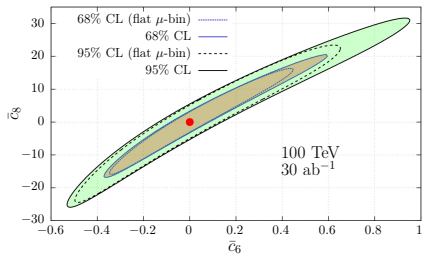
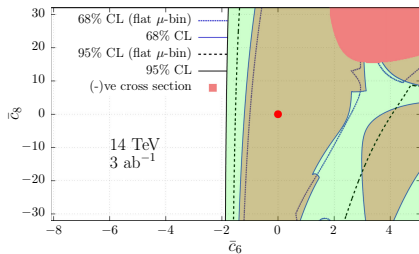
# Constraints at HL-LHC and at 100 TeV: 1P

$$\begin{aligned}\sigma_{\text{NLO}}^{\text{pheno}} &= \sigma_{\text{LO}} + \Delta\sigma_{\bar{c}_6} + \Delta\sigma_{\bar{c}_8}, \\ \sigma_{\text{LO}} &= \sigma_0 + \sigma_1 \bar{c}_6 + \sigma_2 \bar{c}_6^2, \\ \Delta\sigma_{\bar{c}_6} &= \bar{c}_6^2 \left[ \sigma_{30} \bar{c}_6 + \sigma_{40} \bar{c}_6^2 \right] + \tilde{\sigma}_{20} \bar{c}_6^2, \\ \Delta\sigma_{\bar{c}_8} &= \bar{c}_8 \left[ \sigma_{01} + \sigma_{11} \bar{c}_6 + \sigma_{21} \bar{c}_6^2 \right],\end{aligned}$$



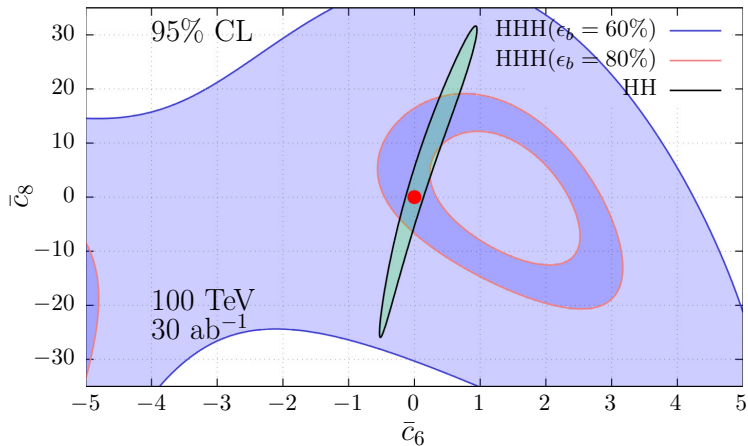
[1811.12366] (See also [1810.04665] )

# Constraints at HL-LHC and at 100 TeV: 2P



[1811.12366]

# Constraints at 100 TeV: $HH$ vs $HHH$



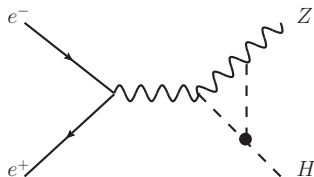
[1811.12366]

# Prospects at $e^+e^-$ colliders

# Indirect determination of $\lambda_3$

We can be sensitive to  $\lambda_3$  in higher order EW corrections in observables of interest: [McCullough: 1312.3322](#).

$$e^+e^- \rightarrow Z + H$$



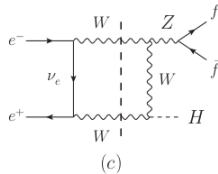
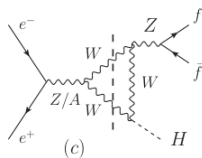
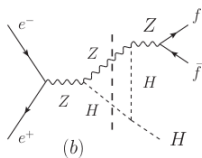
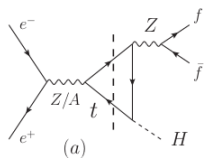
For  $\sqrt{s} = 240$  GeV and  $\mathcal{L} = 10 \text{ ab}^{-1}$ ,  $\kappa_3 \sim 28\%$ .  
(See also [\[1711.03978,1802.07616,1805.03417\]](#))

# Direct determination of $\lambda_3$

$$e^+e^- \rightarrow Z(\rightarrow \ell^+\ell^-) + H$$

$$\frac{d^3\sigma}{d\cos\Theta d\cos\theta d\phi} \rightarrow \underbrace{F_1(1 + \cos^2\theta) + F_2(1 - 3\cos^2\theta) + F_3 \sin 2\theta \cos\phi + F_4 \sin^2\theta \cos 2\phi}_{\text{T-even}}$$

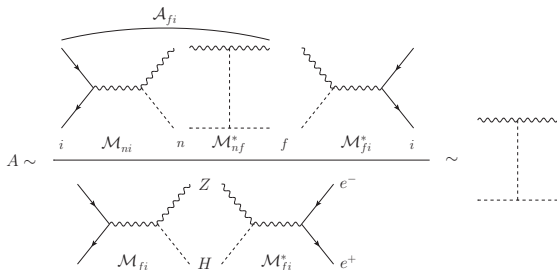
$$+ \underbrace{F_5 \cos\theta + F_6 \sin\theta \cos\phi}_{\text{T-even}} \underbrace{-F_7 \sin\theta \sin\phi - F_8 \sin 2\theta \sin\phi - F_9 \sin^2\theta \sin 2\phi}_{\text{T-odd}}$$



[1812.01576]

# T-odd Asymmetries

$$A_7 \equiv \frac{\sum_{\tau} \xi(\tau) \left( \int_0^1 - \int_{-1}^0 \right) d \cos \Theta F_7(\tau, \cos \Theta)}{\sum_{\tau} \xi(\tau) \int_{-1}^1 d \cos \Theta F_1(\tau, \cos \Theta)},$$

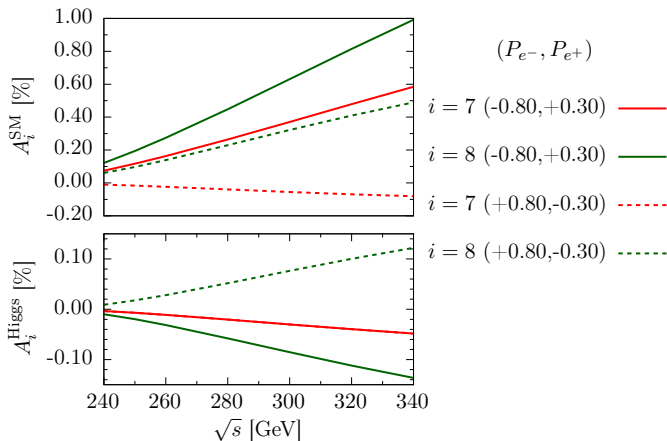


$$\lambda_3 = \lambda_3^{\text{SM}}(1 + \delta_h)$$

[1812.01576]

# SM and BSM asymmetries

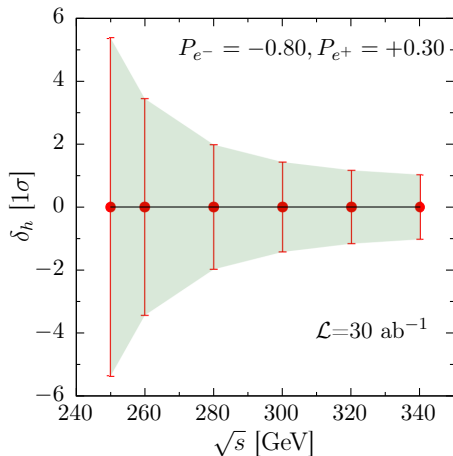
$$A_i^{\text{SM}} = A_i^{\text{Higgs}} + A_i^{\text{Gauge}}; \quad A_i^{\text{BSM}} = \delta_h \times A_i^{\text{Higgs}} + A_i^{\text{SM}}$$



[1812.01576]



# Direct constraint on trilinear from the T-odd asymmetries



[1812.01576]

# Summary and outlook

- Among all the couplings of the Higgs boson, the Higgs self-couplings are poorly known.
- Alternative approaches are being actively sought-for to constrain them using precisely measured observables at the LHC and future colliders.
- A number of studies have shown the complementarity between direct and indirect approaches to probe Higgs self-couplings.
- Efforts are needed to improve the reach by including all the relevant higher order corrections in single and double Higgs production processes.

Thank You.